

## Krivulje v projektivni geometriji

### POVZETEK

Delo predstavi ravninske algebraične krivulje, to so ravninske krivulje opisane z množico rešitev polinoma v dveh spremenljivkah. Predvsem se osredotoči na premice, stožnice ter kubike v projektivnem prostoru. Velik del je namenjen Cayley-Bacharachovem izreku, ki govori o dveh kubičnih krivuljah, ki se sekata v devetih točkah ter konstrukciji grupe na kubični krivulji.

## Curves in projective geometry

### ABSTRACT

Main topic of this paper is to represent plane algebraic curves, planar curves described as the set of solutions of a polynomial in two variables. There are two major parts, the first is dedicated to Cayley-Bacharach theorem, theorem about two cubic curves meeting in nine points. The second part is about construction of a group law on the cubic curves.

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**Ključne besede:** Algebraična geometrija, krivulje v projektivnem prostoru, projektivni prostor, Cayley-Bacharachov izrek, struktura grupe na kubični krivulji.

**Keywords:** Algebraic geometry, curves in projective space, projective space, Cayley-Bacharach theorem, group law on a cubic curve.

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