

POVZETEK

Diplomsko delo je posvečeno študiju delnih urejenosti in nekaterih grafov. S področja teorije delnih urejenosti je predstavljen Dilworthov izrek in nekaj njegovih posledic. Sledi poglavje s področja teorije grafov, kjer so definirani posebni grafi, t.im. primerjalni grafi in njihova karakterizacija. Predstavljeni so tudi popolni grafi, intervalni grafi, osnovni grafi in diagrami. Zanimivo je poglavje o Schnyderjevem izreku, ki povezuje ravninskost grafa in dimenzijo grafu prirejene delne urejenosti. Opisana je incidenčna urejenost grafa in poseben način označevanja točk ravninskega grafa oziroma Schnyderjeva shema za triangulacije.

Klasifikacija (1991): 05 C , 05 C 75, 06 A 07.

Ključne besede: graf, delno urejena množica, Dilworthov izrek, primerjalni graf, ravninski graf, Schnyderjeva označitev, dimenzija.

Math. Subj. Class. (1991): 05 C , 05 C 75, 06 A 07.

Keywords: graph, partially ordered set, Dilworth's theorem, comparability graph, planar graph, Schnyder's labelling, dimension.

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