

Povzetek

To delo predstavi izrek o ločni osi ter teoretično različico algoritma Gilbert–Johnson–Keerthi (GJK) ter njuno uporabo v zaznavi trkov med (konveksnimi) politopi v evklidskem prostoru \mathbb{R}^3 . V prvem delu spoznamo teoretično ozadje afinih prostorov, konveksnih množic, politopov in konveksnih poliedrov, ki nam služi za izpeljavo izreka o ločni osi in GJK-ja ter razumevanje metod, s katerimi se kasneje srečamo. Na koncu so predstavljena še omejujoča območja in prostorske strukture za zmanjšanje časovne zahtevnosti zaznave trkov in števila potencialno prekrivajočih se parov teles.

Abstract

This work presents separating axis theorem (SAT) and the theoretical version of Gilbert–Johnson–Keerthi (GJK) algorithm and their application in collision detection between (convex) polytopes in Euclidean \mathbb{R}^3 space. The first part contains the theoretical foundations from affine spaces, convex sets, polytopes and convex polyhedra required to derive SAT and GJK and for understanding the methods we see later in this work. Finally, bounding volumes and spatial data structures are presented that reduce the time complexity of collision detection and the number of potentially intersecting pairs of objects.

MSC2010: 52A20, 52B10, 52B11, 52B55, 68U20, 68W01

Ključne besede: afini prostor, konveksne množice, konveksni politopi, konveksni poliedri, vsota Minkowskega, ločna os, GJK, zaznava trkov, AABB, k-DOP, OBB, prostorske strukture, mreža vokslov, BSP, sweep-and-prune

Keywords: affine space, convex sets, convex polytopes, convex polyhedra, Minkowski sum, separating axis, GJK, collision detection, AABB, k-DOP, OBB, spatial structures, voxel grid, BSP, sweep-and-prune

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